Carbon sequestration with reforestations and biodiversity-scenic values^{*}

A. Caparrós[†], E. Cerdá[†], P. Ovando[§] and P.Campos[¶]

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Abstract

This paper presents an optimal control model to analyze reforestations with two different species, including commercial values, carbon sequestration and biodiversity or scenic values. We first solve the model qualitatively with general functions and discuss the implications of partial or total internalization of environmental values, showing that internalizing only carbon sequestration may have negative impacts on biodiversity/scenic values. To evaluate the practical relevance, reforestations in the South-west of Spain with cork-oaks and with eucalyptus are compared. We do the analysis with two different carbon crediting methods, the Carbon Flow Method and the Ton Year Accounting Method, showing that the first implies to increase more the forest surface than the second. However, the first implies as well to decrease the proportion of cork-oaks compared to eucalyptus, while the second method increases the proportion of cork-oaks since most of the additional reforestations are done with cork-oaks. A stated preferences study is used to value the impact on visitors of cork-oak and eucalyptus reforestations. We show that if these values were internalized the equilibrium values would imply a significantly higher amount of surface devoted to cork-oaks than to eucalyptus, even if carbon sequestration would be internalized.

Key words: optimal control, forests, carbon sequestration, biodiversity values, scenic values, stated preferences, carbon accounting.

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[†]Spanish Council for Scientific Research (CSIC), Spain. E-mail: acaparros@ieg.csic.es. Corresponding author.

[‡]Department of Economic Analysis. University Complutense Madrid, Spain.

[§]Spanish Council for Scientific Research (CSIC), Spain.

 $[\]P{\ensuremath{\mathsf{Spanish}}}$ Council for Scientific Research (CSIC), Spain.

1 Introduction

Countries which have ratified the Kyoto Protocol, a development of the United Nations Framework Convention on Climate Change, will need to reduce their greenhouse gas emissions, on average, to 5% below 1990 levels by 2012. One of the alternatives included in the Kyoto Protocol to achieve this goal is to plant trees, since trees sequester carbon from the atmosphere by growing and reduce therefore carbon dioxide concentrations. This is know as 'afforestation and reforestation' in the terminology used in the Kyoto Protocol and the Marrakech Accords, an agreement that completes the Protocol. Although it is not yet sure if the Kyoto Protocol will continue after 2012 in its current form, it is almost sure that some kind of international policy on climate change will continue, and the rules to be set up for reforestation programs will probably rely heavily on those developed for the Kyoto Protocol, giving the enormous amount of negotiation effort already invested into them¹.

It is usually accepted that biodiversity increases when degraded and agricultural lands are converted into forests (IPCC, 2000). However, this is only true in regard to indigenous forests and not when the 'reforestation' is actually the setting up of rapidly growing alien species plantations. It is also not true where pre-existing land uses have high biodiversity values (IPCC, 2000). Matthews et al. (2002) have quantified bird biodiversity associated to reforestations in the United States and have found further evidence of the potential negative impacts of reforestation regimes. Therefore, the 'afforestation and reforestation' alternative may potentially conflict with the goal of the Convention on Biodiversity, since incentives to increase carbon sequestration may favor the use of fast growing alien species, which can potentially be negative for biodiversity, as indicated in Caparrós and Jacquemont (2003 and 2005). The authors also show that neither the convention on climate change (UNFCCC) nor the convention on biodiversity (CBD) have adequate mechanisms to avoid this possibility, especially in the case of the 'afforestations and reforestation' alternative since most of the limits established for carbon sequestration alternatives do not affect this option². Although it has received less attention, a similar argument can be elaborated linking carbon sequestration and scenic values, since fast growing plantations tend to have lower scenic beauty. In this article we will treat these values indistinctly, as values that are currently not internalized by markets and that will probably remain outside of markets in the near future (while carbon

¹The United States have decided not to ratify the Kyoto Protocol, but during the negotiations of the Protocol and the Marrakech Accords they were one of the Parties more clearly advocating for the extensive use of carbon sequestration, or 'sinks' alternatives, so that forest alternatives will continue to be a fundamental part of their carbon policy (Richards et al., 2006).

² 'Forest management' has a strong quantitative limit that probably will imply that no incentives are established by the Annex I countries since the limit will be reached anyway. In addition, the definition given explicitly includes a reference to biodiversity. Finally, most forest management options to increase carbon sequestration tend to increase forest rotations and this is generally positive or biodiversity. The remaining LULUCF alternatives are expected to be less important. See Caparrós and Jacquemont (2003 and 2005) for more details.

sequestration values are about to be internalized).

According to the Marrakech Accords, Parties can issue credits through afforestation and reforestation by means of art. 3.3 of the Kyoto Protocol if the land is located in an Annex I country³ that ratifies the Protocol (or eventually via art. 6 and Joint Implementation), and by means of art. 12 (Clean Development Mechanism) if the land is located in any Non-Annex I Party. In the first case, each country can decide how to incentivate carbon sequestration in its own land. What is going to matter at the international level is the total carbon budget of the country, since the Kyoto targets are based on net emissions. Therefore, a reasonable incentive mechanism to be set up by Annex-I governments is what is known as the 'Carbon Flow Method' (CFM). This method was proposed in the early literature on the impact of carbon sequestration on optimal rotations (Englin an Callaway (1993) or Van Kooten et al. (1995)) and essentially implies that the forest owner gets paid by the government⁴ (a subsidy) when carbon sequestration takes place and has to pay (a tax) when carbon is released (Feng et al (2002) describe a similar system calling it the 'pay-as-you-go' method). The value of this carbon subsidy-tax is set equal to the carbon price attached to emissions of CO_2 . Richards et al (2006) also present this method as one of the best alternatives to be used in the US. An alternative method, or set of methods, is well represented by what is known as the 'Ton Year Accounting Method' (TYAM), see Moura-Costa and Wilson (2000). This method implies to pay a given amount to the forest owner each year as long as the carbon stays in the forest. The price to be paid is based on the carbon emission price and an equivalence factor (ε) that captures the benefit associated to sequestering one ton of CO_2 in forest biomass for one year (this equivalence factor is estimated based on the cumulative radiative forcing of an emission of CO_2 over a 100-years time horizon). An essentially similar method is the carbon 'rental fee' used in Sohngen and Mendelsohn (2003), where the forest owner gets paid a fee for each ton of carbon stored for one year. Although the method used to calculate this fee in Sonhagen and Mendelsohn's paper is totally different, based on the expected increase in carbon emission prices, what matters for our purposes is that the owner gets paid for the total number of tons of carbon sequestered (not for the increase in carbon) and that the amount paid is substantially lower than the carbon price. The 'variable-lenght-contract' method described in Feng et al. (2002) is also similar to the TYAM, as the authors recognize. Thus, by analyzing the outcome with the CFM and the TYAM we are able to cover most of the methods proposed so far in the literature.

For credits earned by CDM projects two methods have finally been accepted within the Kyoto-Marrakech framework: the t-CERs and the l-CERs (Olshewski and Benítez, 2005). The main difference between the two crediting procedures is the lifetime of the credit, 5 years in the case of the t-CER and up to 30 years with the l-CERs (both methods are subject to a maximum time limit of 60 years). The t-CER method can be seen as a variation of the TYAM

³Essentially the OECD countries and the economies in transition

 $^{^4\,{\}rm For}$ both methods (CFM and TYAM) the money could actually come from a well defined emission trading scheme.

'type' of methods (paying for the standing forest, not for growth), with the particularity that the price is paid every 5 years and that the contract has a maximum time limit. Nevertheless, although our model is general enough to be applied within the CDM framework, we will focus on the situation in an Annex-I country (Spain in the application) and discuss the two methods described in the previous paragraph.

Van Kooten (2000) proposed an optimal control model to evaluate carbon sequestration via 'afforestation and reforestation' with one single species, without taking into account biodiversity or scenic values. Applying this model to Canada, the author makes a strong argument in favor of large scale plantations using fast growing species.

The model that we are going to present here develops this model in three ways: (i) we include a second tree species, what implies to have a second state variable and a second control variable, (ii) we include biodiversity-scenic values in the analysis, and (iii) we allow for more general functions. We characterize the steady-state of the model and show phase diagrams under some additional assumptions (constant value of pasture land). We then apply it to data for the South-west of Spain and discuss the outcomes with the two carbon accounting methods described above.

Moons *et al.* (2004) also deal, using a GIS-based model, with the establishment of new forests for carbon sequestration purposes, including recreation and other values in the analysis. Their model is solved numerically and highlights the empirical importance of taking into account recreational values. In Caparrós *et al.* (2003) recreational values and carbon sequestration values are optimized jointly while determining the optimal rotation, but this model does not deal with reforestations. The remaining and extensive literature on reforestations set up for carbon sequestration purposes does not incorporate neither biodiversity nor recreational or scenic values in the analysis (for a review, see Richards and Stokes (2004)).

In the applied section of this paper, we compare reforestations in the Southwest of Spain with two different species: cork-oak, a native slow growing species, and eucalyptus, an alien fast growing species that has been used in this area in the past. The first species, or the ecosystem associated with it, is assumed to have positive biodiversity values while the second is assumed to have a negative impact in terms of biodiversity, at least in the area under consideration. Oaks (cork-oaks and holm-oaks) are the main tree species in the Mediterranean forests, one of the hot-spots for biodiversity in the world. Nevertheless, since biodiversity is not easy to monetarize we have estimated the impact on the visitors welfare of a reforestation with either one of these species using stated preferences methods. We do not claim to be able to separate biodiversity values from scenic values, since visitors are probably considering both values when comparing the two species, and we will thus refer to biodiversity-scenic values in the application. The results show that visitors perceive reforestations with cork-oaks as having a positive impact on their welfare while they perceive reforestations with euclyptus as having a negative impact on their welfare. To put a dollar value on these welfare changes we have conducted a choice experiment to value the contribution of cork-oak reforestations to the welfare of the visitors. Although we have less confidence in the results for the reasons discussed below, we have also tried to measure the impact of reforestations with eucalyptus (and with cork-oaks) using the contingent valuation method. To integrate these values into our model, we have assumed that a share of these welfare changes could be internalized through additional subsidies for cork-oaks or through compensations to refrain from using eucalyptus (see below).

Turning to the results of our applied model, we first show that with current market values reforestations with cork-oaks would not take place even if carbon sequestration values were internalized. Nevertheless, with the current system of subsidies for cork-oak reforestation (which was not set up for carbon purposes but for other environmental values; and which is safe to assume that it will continue in the future) the new incentives for carbon sequestration would significantly increase the optimal amount of cork-oaks in a scenario without competition with euclyptus. If we allow for competition with euclyptus, we show that both incentive mechanism described above to foster carbon sequestration (CFM and TYAM) imply an increase in the surface devoted to forest, although this increase is higher with the CFM method (yielding a steady-state were pasture almost disappears for high carbon prices). However, we also show that the CFM method implies to decrease the proportion of cork-oak over eucalyptus, while the TYAM method yields the opposite result, increasing the proportion of cork-oak over eucalyptus (compared to the equilibrium with no carbon sequestration incentives). In fact, with the TYAM method most of the increase in surface takes place using cork-oaks. Furthermore, if biodiversityscenic values were internalized, the amount of surface devoted to eucalyptus would be significantly smaller than the amount devoted to cork-oaks without carbon sequestration values, but also with carbon internalized using either one of the accounting methods discussed in this paper (except for the CFM and high carbon prices).

The rest of the article is organized as follows. Section 2 presents the model and discusses it with general functional forms. We show that the equilibrium will generally be a saddle point, and analyze qualitatively the optimal path under the assumption that pasture land has constant returns to scale. Section 3 contains the application in the South-west of Spain. We first analyze the model with the quadratic functions used in the application, dropping the assumption that the marginal value of pasture is constant. The section continues by showing the results obtained internalizing only carbon sequestration and then moves on to show the results obtained internalizing biodiversity-scenic values as well. Section 4 concludes.

2 The model

We assume that the agent (forest owner) can choose between two types of forest, and that type 1 has greater biodiversity-scenic values while type 2 has greater carbon sequestration potential. A typical example of this situation is when reforestation with a natural indigenous species alternative (forest type 1) is compared with a fast growing alien species (forest type 2). In the case study presented below we compare reforestations with cork-oaks (type 1) and with eucalyptus (type 2) in the South-west of Spain.

Define: L= total land available for reforestation; $f_0(t)$ = pasture land at time t; $f_1(t)$ = reforested land of forest type 1; $f_2(t)$ = reforested land of forest type 2. To simplify we can eliminate $f_0(t)$ from the model by setting $f_0(t) =$ $L - f_1(t) - f_2(t)$ and leave f_1 and f_2 as state variables. Obviously, f_i cannot have negative values. Nevertheless, for simplicity, we analyze the problem without explicitly incorporating this restriction and check afterwards our results for nonnegativity.

Define further: r = discount rate, $u_i(t) = \text{total area reforested at time } t$ of forest type i (i = 1, 2) (control variables), and $K_i(u_i) = \text{reforestation cost}$ for forest type i (i = 1, 2), a function of the amount of land reforested in a given year. The control variable $u_i(t)$ refers to the amount of new land devoted to forest (although u could imply a deforestation for some initial conditions we will focus on situations where it implies reforestations, see below). We assume $K'_i(u_i) > 0$ and $K''_i(u_i) > 0$ (e.g. as specialized labor becomes scarce, salaries increase).

Finally, define F_i $(f_i)(i = 0, 1, 2)$ as space-related functions showing the annual net return values for pasture land (i = 0) or for each type of forest i (i = 1, 2). We assume⁵ $F'_i > 0$ and $F''_i < 0$. These functions are supposed to have three terms: $F_i(f_i) = W_i(f_i) + C_i(f_i) + B_i(f_i)$. Where: W_i, C_i and B_i represent annual net returns associated with commercial uses (timber, cork, fire-wood, grazing resources rent etc.), carbon sequestration and biodiversityscenic values respectively (we will discuss below the internalization of the latter values). Forest-related data are strongly time-related but for modeling reasons it is interesting to annualize them, ensuring that investment incentives are not changed (Van Kooten, 2000). That is, following Van Kooten we will assume that once a piece of land is converted it stays in the new status, so that we can find an annualized value that is equivalent to the future stream of benefits associated to this type of land use⁶. This is the same assumption made in Van't Veld and Plantinga (2005) and essentially the same than the assumption made in Feng et al. (2003). Since we start in a situation where $f_1(0) = f_2(0) = 0$ (in land that is suitable for the 'afforestation and reforestation alternative) this assumption is reasonable in empirical terms, since the high costs associated with a reforestation ensure that the conversion to a particular forest type is only worthwhile if the forests stays for a sufficiently long period of time.

The objective function is:

 $^{^{5}}$ This assumption implies that each species or type of use has different optimal growth areas, which is a reasonable assumption in most cases. For large scale reforestations price effects can also explain this functional forms.

⁶Calling z(t) to the real flow of net benefits associated to any of the values described above (z(t) could also be decomposed in quantity times price), the present value of the investment is: $PV_z = \int_0^\infty z(t)e^{-rt}dt$. And the annualised value Z which assures equal investment incentives checks $Z = rPV_z = r \int_0^\infty z(t)e^{-rt}dt$.

$$MaxV = \int_0^\infty \Pi_t e^{-rt} dt$$

$$\Pi_t = F_1(f_{1t}) - K_1(u_{1t}) + F_2(f_{2t}) - K_2(u_{2t}) + F_0(L - f_{1t} - f_{2t})$$

 $\operatorname{st.}$

$$\dot{f}_1 = u_1 \tag{1}$$

$$\dot{f}_2 = u_2 \tag{2}$$

And initial conditions: $f_1(0) = 0$ and $f_2(0) = 0$. Although it is not necessary for the model itself, to apply the model to the 'afforestation and reforestation' alternative within the Kyoto Protocol we have to assume that $f_1(0) = f_2(0) = 0$, since only areas not covered by forests in 1990 are eligible.

Using the current-value Hamiltonian and dropping time notation the Pontryagin maximum principle conditions are:

$$MaxH_c = \Pi + \lambda_1 u_1 + \lambda_2 u_2, \tag{3}$$

$$\dot{\lambda}_1 = r\lambda_1 - \frac{\partial H_c}{\partial f_1} = r\lambda_1 - \left[F_1'(f_1) + \frac{\partial F_0(L - f_1 - f_2)}{\partial f_1}\right]$$
(4)

$$\dot{\lambda}_2 = r\lambda_2 - \frac{\partial H_c}{\partial f_2} = r\lambda_2 - \left[F_2'(f_2) + \frac{\partial F_0(L - f_1 - f_2)}{\partial f_2}\right]$$
(5)

equations (1) and (2) and the transversality condition $\lim_{t\to\infty} \lambda_i(t) = 0, i = 1, 2$. Π is a concave function, since it is the sum of concave functions and con-

 Π is a concave function, since it is the sum of concave functions and convex functions (with a negative sign). In addition, the equations of motion for the state variables are linear in the control variables. Thus, the Mangasarian sufficient conditions will hold.

Equation (3) implies:

$$\frac{\partial H_c}{\partial u_1} = -K_1'(u_1) + \lambda_1 = 0$$
$$\frac{\partial H_c}{\partial u_2} = -K_2'(u_2) + \lambda_2 = 0$$

Solving for λ_1 and λ_2 :

$$\lambda_1 = K_1'(u_1) \tag{6}$$

$$\lambda_2 = K_2'(u_2) \tag{7}$$

And in the steady-state we will have $\dot{\lambda}_1 = \dot{\lambda}_2 = \dot{f}_1 = \dot{f}_1 = u_1 = u_2 = 0$. Hence, substituting (6) (respectively (7)) in (4) (respectively (5)) we obtain the following FOC for the steady-state:

$$\frac{F_1'(f_1)}{r} - K_1'(0) = \frac{F_0'(L - f_1 - f_2)}{r}$$
(8)

$$\frac{F_2'(f_2)}{r} - K_2'(0) = \frac{F_0'(L - f_1 - f_2)}{r}$$
(9)

where:

$$F_0'(L - f_1 - f_2) = -\frac{\partial F_0(L - f_1 - f_2)}{\partial f_1} = -\frac{\partial F_0(L - f_1 - f_2)}{\partial f_2}$$

Taking (8) and (9) together we have:

$$\frac{F_1'(f_1)}{r} - K_1'(0) = \frac{F_2'(f_2)}{r} - K_2'(0) = \frac{F_0'(L - f_1 - f_2)}{r}$$
(10)

The interpretation of equation (10) follows conventional lines. In the steadystate equilibrium the stream of net revenues associated with the reforestation of one additional hectare of forest type 1 has to be equal to the revenues associated to one additional hectare reforested with forest type 2, and to the revenues associated to the use of that hectare as pastureland.

To find the dynamic path we derive (6) and (7) with respect to time:

$$\dot{\lambda}_1 = K_1''(u_1)\dot{u}_1$$
 (11)

$$\dot{\lambda}_2 = K_2''(u_2)\dot{u}_2$$
 (12)

Substituting in (4) (respectively (5)):

$$\dot{u}_1 = \frac{rK_1'(u_1) - [F_1'(f_1) - F_0'(L - f_1 - f_2)]}{K_1''(u_1)}$$
(13)

$$\dot{u}_2 = \frac{rK_2'(u_2) - [F_2'(f_2) - F_0'(L - f_1 - f_2)]}{K_2''(u_2)}$$
(14)

2.1 Saddle point

Dockner (1985) gives necessary and sufficient conditions for a system with two state variables to have a saddle point (assuming r > 0). These conditions imply (i) D < 0 and (ii) $0 < |J_E| \le (D/2)^2$, where D is as defined below and $|J_E|$ is the determinant of the Jacobian matrix of the system evaluated at the equilibrium point.

The determinant of the Jacobian matrix for the system formed by (1)(2)(13) and (14) evaluated at the equilibrium point is:

$$|J_E| = \begin{vmatrix} \frac{\partial \dot{f}_1}{\partial f_1} & \frac{\partial \dot{f}_1}{\partial f_2} & \frac{\partial \dot{f}_1}{\partial u_1} & \frac{\partial \dot{f}_1}{\partial u_2} \\ \frac{\partial \dot{f}_2}{\partial f_1} & \frac{\partial f_2}{\partial f_2} & \frac{\partial \dot{f}_2}{\partial u_1} & \frac{\partial \dot{f}_2}{\partial u_2} \\ \frac{\partial \dot{u}_1}{\partial f_1} & \frac{\partial \dot{u}_1}{\partial f_2} & \frac{\partial \dot{u}_1}{\partial u_1} & \frac{\partial \dot{u}_1}{\partial u_2} \\ \frac{\partial \dot{u}_2}{\partial \dot{t}_2} & \frac{\partial \dot{u}_2}{\partial t_2} & \frac{\partial \dot{u}_2}{\partial u_1} & \frac{\partial \dot{u}_2}{\partial u_2} \\ \frac{\partial \dot{u}_2}{\partial f_1} & \frac{\partial \dot{u}_2}{\partial f_2} & \frac{\partial \dot{u}_2}{\partial u_1} & \frac{\partial \dot{u}_2}{\partial u_2} \\ \frac{\partial \dot{u}_2}{\partial f_1} & \frac{\partial \dot{u}_2}{\partial f_2} & \frac{\partial \dot{u}_2}{\partial u_2} & \frac{\partial \dot{u}_2}{\partial u_2} \\ \frac{\partial \dot{u}_2}{\partial f_1} & \frac{\partial \dot{u}_2}{\partial f_2} & \frac{\partial \dot{u}_2}{\partial u_2} & \frac{\partial \dot{u}_2}{\partial u_2} \\ \frac{\partial \dot{u}_2}{\partial f_1} & \frac{\partial \dot{u}_2}{\partial f_2} & \frac{\partial \dot{u}_2}{\partial u_2} & \frac{\partial \dot{u}_2}{\partial u_2} \\ \frac{\partial \dot{u}_2}{\partial f_1} & \frac{\partial \dot{u}_2}{\partial f_2} & \frac{\partial \dot{u}_2}{\partial u_2} & \frac{\partial \dot{u}_2}{\partial u_2} \\ \frac{\partial \dot{u}_2}{\partial f_1} & \frac{\partial \dot{u}_2}{\partial f_2} & \frac{\partial \dot{u}_2}{\partial u_2} & \frac{\partial \dot{u}_2}{\partial u_2} \\ \frac{\partial \dot{u}_2}{\partial f_1} & \frac{\partial \dot{u}_2}{\partial f_2} & \frac{\partial \dot{u}_2}{\partial u_2} & \frac{\partial \dot{u}_2}{\partial u_2} \\ \frac{\partial \dot{u}_2}{\partial f_1} & \frac{\partial \dot{u}_2}{\partial f_2} & \frac{\partial \dot{u}_2}{\partial u_2} & \frac{\partial \dot{u}_2}{\partial u_2} \\ \frac{\partial \dot{u}_2}{\partial f_1} & \frac{\partial \dot{u}_2}{\partial f_2} & \frac{\partial \dot{u}_2}{\partial u_2} & \frac{\partial \dot{u}_2}{\partial u_2} \\ \frac{\partial \dot{u}_2}{\partial f_1} & \frac{\partial \dot{u}_2}{\partial f_2} & \frac{\partial \dot{u}_2}{\partial u_2} & \frac{\partial \dot{u}_2}{\partial u_2} \\ \frac{\partial \dot{u}_2}{\partial f_1} & \frac{\partial \dot{u}_2}{\partial h_2} & \frac{\partial \dot{u}_2}{\partial h_2} & \frac{\partial \dot{u}_2}{\partial h_2} \\ \frac{\partial \dot{u}_2}{\partial h_2} & \frac{\partial \dot{u}_2}{\partial h_2} & \frac{\partial \dot{u}_2}{\partial h_2} & \frac{\partial \dot{u}_2}{\partial h_2} \\ \end{array} \right$$

Since $\frac{\partial \dot{f}_i}{\partial f_j} = \frac{\partial \dot{f}_i}{\partial f_i} = \frac{\partial \dot{u}_i}{\partial u_j} = 0$, and $\frac{\partial \dot{f}_i}{\partial u_i} = 1$ we have:

$$|J_E| = \frac{\partial \dot{u}_1}{\partial f_1} \frac{\partial \dot{u}_2}{\partial f_2} - \frac{\partial \dot{u}_1}{\partial f_2} \frac{\partial \dot{u}_2}{\partial f_1} > 0$$
(15)

D is defined as follows (Dockner, 1985);

$$D = \begin{vmatrix} \frac{\partial f_1}{\partial f_1} & \frac{\partial f_1}{\partial u_1} \\ \frac{\partial \dot{u}_1}{\partial f_1} & \frac{\partial \dot{u}_1}{\partial u_1} \end{vmatrix} + \begin{vmatrix} \frac{\partial f_2}{\partial f_2} & \frac{\partial f_2}{\partial u_2} \\ \frac{\partial \dot{u}_2}{\partial f_2} & \frac{\partial \dot{u}_2}{\partial u_2} \end{vmatrix} + 2 \begin{vmatrix} \frac{\partial f_1}{\partial f_2} & \frac{\partial f_1}{\partial u_2} \\ \frac{\partial \dot{u}_1}{\partial f_2} & \frac{\partial \dot{u}_1}{\partial u_2} \end{vmatrix}$$

And in our system this simplifies to:

$$D = -\frac{\partial \dot{u}_1}{\partial f_1} - \frac{\partial \dot{u}_2}{\partial f_2} < 0 \tag{16}$$

Comparing (15) and (16) we can see that $|J_E| \leq (D/2)^2$ also holds, since we can re-write it as

$$\frac{\partial \dot{u}_1}{\partial f_1} \frac{\partial \dot{u}_2}{\partial f_2} - \frac{\partial \dot{u}_1}{\partial f_2} \frac{\partial \dot{u}_2}{\partial f_1} \le \left(\frac{\frac{\partial \dot{u}_1}{\partial f_1}}{2}\right)^2 + \left(\frac{\frac{\partial \dot{u}_2}{\partial f_2}}{2}\right)^2 + \frac{1}{2} \frac{\partial \dot{u}_1}{\partial f_1} \frac{\partial \dot{u}_2}{\partial f_2}$$

or

$$0 \le \left(\frac{\partial \dot{u}_1}{\partial f_1} - \frac{\partial \dot{u}_2}{\partial f_2}\right)^2 + 4 \frac{\partial \dot{u}_1}{\partial f_2} \frac{\partial \dot{u}_2}{\partial f_1}$$

and this inequality is always checked.

Thus, the system will generally have a saddle-point, the best kind of stability that we can expect in this type of two state-variable dynamic systems (Dockner, 1985).

2.2Phase-diagram

Setting $F'_0(f_0) = \alpha \ge 0, \forall f_0$ (that is, the marginal value of pasture land is constant) we can analyze graphically the paths of both reforestations independently since both systems described by equations (13) and (14) are 'decoupled'⁷. We will analyze the phase-diagram for species 1 (for species 2 the analysis would be analogous).

Since $F'_1(f_1) = X > 0$ and $K'_1(u_1) = Y > 0$ are monotonic functions we can write $F'_1(X) = f_1 > 0$ and $K'_1^{-1}(Y) = u_1 > 0$. And since $F''_1(f_1) < 0$ and $K''_1(u_1) > 0$, we know that $(F'_1)'(X) < 0$ and $(K'_1)'(Y) > 0$. From (1) we can show that the $\dot{f}_1 = 0$ isocline follows the f_1 axis:

$$\dot{f}_1 = 0 \Leftrightarrow u_1 = 0$$

And from (13) we have:

$$\dot{u}_1 = 0 \Leftrightarrow F_1'(f_1) = rK_1'(u_1) + \alpha \tag{17}$$

⁷However, this implies indirectly that the land restriction is not taken into account.

Thus:

$$f_1 = F_1'^{-1} \left(r K_1'(u_1) + \alpha \right) > 0$$

Deriving with respect to u_1 :

$$\frac{\partial f_1}{\partial u_1} = \frac{\partial F_1^{\prime - 1}}{\partial X} \frac{\partial X}{\partial u_1} = \frac{\partial F_1^{\prime - 1}}{\partial \left(rK_1^{\prime}(u_1) + \alpha \right)} rK_1^{\prime\prime}(u_1) < 0$$

To plot the $\dot{u}_1 = 0$ isocline we look for the values for $f_1 = 0$ and for $u_1 = 0$: With $f_1 = 0$ (from (17)):

$$u_1 = K_1'^{-1} \left(\frac{F_1'(0) - \alpha}{r} \right)$$

Thus $u_1 > 0$ if $F'_1(0) > \alpha$. I.e. the reforestation in a given year with species 1 will be positive if the marginal value of the first unit of land reforested with this species 1 is higher than the marginal value of a unit of pasture land (which is supposed to be constant). We assume that this holds, otherwise no reforestation would occur at all.

For $u_1 = 0$:

$$f_1 = F_1'^{-1}(rK_1(0) + \alpha) > 0$$

In addition, we have

$$\begin{array}{lll} \frac{\partial f_1}{\partial u_1} & = & 1 > 0 \\ \frac{\partial \dot{u}_1}{\partial f_1} & = & \frac{-F_1''(f_1)}{K_1''(u_1)} > 0 \end{array}$$

Plotting this information we get figure 1.

[Figure 1 here]

The long-term equilibrium is the intersection of the $\dot{u}_1 = 0$ isocline and the $\dot{f}_1 = 0$ isocline. That is, in the long-term equilibrium the amount of forest type 1 is: $f_1^* = F_1'^{-1}(rK_1(0) + \alpha) > 0$ (since at the equilibrium $u_1 = 0$). Given the streamlines this will be a saddle point. If the initial amount of forest type 1 (z_1) is lower than the optimal amount f_1^* the optimal approach is to reforest forest type 1 (a positive u_1) following the stable branch northwest of the long-term equilibrium. If the initial amount of forest type 1 is higher than f_1^* the optimal approach is to follow⁸ the stable branch southeast of the long-term equilibrium (i.e. to reduce the amount of forest type 1, a negative u_1).

To check the saddle-point we can write the Jacobian determinant for this sub-system with one state-variable:

 $^{^{8}}$ In any case, the optimal approach never implies to reforest first and deforest afterwards, so that the annualization of the revenues as described above does not change the investment incentives.

$$J|_{E} = \begin{vmatrix} \frac{\partial f_{1}}{\partial f_{1}} & \frac{\partial f_{1}}{\partial u_{1}} \\ \frac{\partial u_{1}}{\partial f_{1}} & \frac{\partial u_{1}}{\partial u_{1}} \end{vmatrix} = \begin{vmatrix} 0 & 1 \\ \frac{\partial \dot{u}_{1}}{\partial f_{1}} & \frac{\partial \dot{u}_{1}}{\partial u_{1}} \end{vmatrix} < 0$$

A sufficient condition for a saddle-point with one state variable is $|J_E| < 0$. Since $\partial \dot{u}_1 / \partial f_1 > 0$, we have $|J_E| < 0$.

2.3 Commercial, carbon and biodiversity-scenic values

Until now we have discussed the system focusing on the overall valuation function (F). In this section we will discuss the impact of different values for conventional commercial uses (timber, cork, firewood), carbon sequestration (a value that might become a market value in the future) and biodiversity-scenic values. To make things interesting, we will assume $B'_1 > B'_2$, and $C'_1 < C'_2 \forall f$ (i.e. species 1 has higher marginal values for biodiversity and species 2 has higher marginal values for carbon sequestration).

Building on the results of the last section, and recalling the additive form of the valuation function assumed, we can compare the optimal amount of space devoted to each species in the equilibrium:

$$\frac{f_1^*}{f_2^*} = \frac{F_1'^{-1}(rK_1(0) + \alpha)}{F_2'^{-1}(rK_2(0) + \alpha)} = \frac{(W_1' + C_1' + B_1')^{-1}(rK_1(0) + \alpha)}{(W_2' + C_2' + B_2')^{-1}(rK_2(0) + \alpha)}$$

In the current market situation only the timber values (W) will be considered. In the future, carbon may become a market value and W and C will be considered by private decision makers. From a social point of view, however, W, C and B should be taken into account. Let us assume, to focus on the differences in carbon and biodiversity values between species 1 and 2, that current market values (W) are equal in both species and that reforestation costs are also equal for both species. In this setting, we have $\left(\frac{f_1^*}{f_2^*}\right)_W = 1$, where the sub-index of the bracket indicates the value(s) considered (only W). Since we have assumed $C'_1 < C'_2$, we will have $\left(\frac{f_1^*}{f_2^*}\right)_{WC} < 1$, if current (timber) and future (carbon) market values are taken into account. Given $B'_1 > B'_2$, if current market values (timber) and biodiversity-scenic values are taken into account we have $\left(\frac{f_1^*}{f_2^*}\right)_{WB} > 1$. This is the situation that a central planner should take into account today (if we assume that carbon sequestration plays no role for the time being). Finally, the value of $\left(\frac{f_1^*}{f_2^*}\right)_{WCB}$ depends on the relative importance of carbon and biodiversity-scenic values. Figure 2 depicts this situation (in this figure biodiversity values for species 2 are supposed to be negative).

[Figure 2 here]

That is, we might have a situation where future market forces (timber plus carbon) favor species 2 while present market forces equalize the amounts of both species, and social benefits (timber, carbon sequestration and biodiversityscenic values) would favor species 1. If only timber and biodiversity-scenic values are taken into account (probably the social values currently considered) the relative amount of species 1 in the equilibrium should even be bigger. In addition, these values (especially scenic values) are local by their nature while carbon sequestration benefits are global. Thus, implementing an incentive for carbon sequestration might, in this particular case, imply a stress for local social benefits.

However, the general forms used in the discussion so far do not allow us to say if this situation is relevant in the real world. Thus, we will apply the model just described to a multiple-use forests in Spain.

3 Application

Since we need to specify particular functions to apply the model we will first discuss the model with the particular functions to be used in the application. We will then apply the model to a multiple-use forest in Spain: the Alcornocales Natural Park (located in the South-west of Spain). This Natural Park has an extension of about 170,000 hectares and is partially covered by cork-oaks, which have suffered a slow deforestation process in the last decades. Forests (mainly cork-oaks) cover currently about 53% of the total surface of the area and eucalyptus have also been used in the past in this area for reforestation⁹. Since we are analyzing the option that could be considered as 'afforestation and reforestations' within the Kyoto Protocol we have to focus on the areas that were not covered by trees in 1990. This leaves us with about 80,000 hectare.

3.1 Quadratic functions

We continue the analysis assuming particular functional forms. This will allow us to relax again the assumption that marginal values for pasture land are constant (which we only used to draw the phase diagram). We assume quadratic functions, since these functions are well suited to depict the decreasing returns typical of forestry outputs (areas most suited for a given species are reforested first). In addition, the additive property of the coefficients in these type of functions is very convenient for the discussion on the three different types of benefits generated by the forests under consideration. Finally, the quadratic form is well suited to adapt the data obtained through a choice experiment for biodiversity-scenic values (see table 2 below).

For the valuation functions we have:

⁹Right now plantations with eucalyptus are not allowed in this area due to environmental restrictions. Within our model this implies that taking into account the values for W and B the government has decided to preclude the use of eucalyptus, but not using market values. We are thus studying the impact of relaxing this environmental constraint. Alternatively, our results can be seen as applying to areas where this environmental contraint is not in place.

$$F_{i} = a_{i0} + a_{i1}f_{i} + (1/2)a_{i2}f_{i}^{2}, \quad (i = 0, 1, 2)$$

$$F_{i}' = a_{i1} + a_{i2}f_{i} > 0 \Rightarrow a_{i1} > 0$$

$$F_{i}'' = a_{i2} \le 0 \Rightarrow a_{i2} \le 0$$

$$a_{i0} \ge 0$$

For reforestation costs we set $k_{ij} \ge 0$ (i = 1, 2; j = 0, 1, 2), since $K'_i(u_i) > 0$ and $K''_i(u_i) > 0$. In addition, for the valuations functions (F_i) a negative value may well have a economic sense for large numbers of f_i , but negative reforestation costs have no sense.

$$K_i = k_{i0} + k_{i1}u_i + (1/2)k_{i2}u_i^2$$
 $(i = 1, 2)$

In addition, we have:

$$F_{i} = W_{i} + C_{i} + B_{i}$$

$$W_{i} = w_{i0} + w_{i1}f_{i} + (1/2)w_{i2}f_{i}^{2}$$

$$C_{i} = c_{i0} + c_{i1}f_{i} + (1/2)c_{i2}f_{i}^{2}$$

$$B_{i} = b_{i0} + b_{i1}f_{i} + (1/2)b_{i2}f_{i}^{2}$$

Thus:

$$a_{ij} = w_{ij} + c_{ij} + s_{ij}$$

The FOC are now:

a

$$a_{11} + a_{12}f_1 - rk_{11} = a_{01} + a_{02}(L - f_1 - f_2)$$
(18)

$$a_{11} + a_{22}f_2 - rk_{21} = a_{01} + a_{02}(L - f_1 - f_2)$$
(19)

Solving for f_1 and f_2 using Cramer's rule and rearranging:

$$f_1^* = \frac{a_{02}[(a_{11} - rk_{11}) - (a_{21} - rk_{21})] + a_{22}[(a_{11} - rk_{11}) - (a_{01} + a_{02}L)]}{-a_{12}a_{22} - a_{12}a_{02} - a_{02}a_{22}}$$
$$f_2^* = \frac{a_{02}[(a_{21} - rk_{21}) - (a_{11} - rk_{11})] + a_{12}[(a_{21} - rk_{21}) - (a_{01} + a_{02}L)]}{-a_{12}a_{22} - a_{12}a_{02} - a_{02}a_{22}}$$

Since $a_{i2} \leq 0$ the denominator is negative. In the numerator all the terms in brackets are positive. The second square bracket in each expression should be positive, since it is the difference between the net marginal benefit for the first unit of land (the best) with one of the forest species and the marginal benefit for pasture for the last unit of land (L). If this difference is not positive, no reforestation will occur at all for this particular species. The first square bracket will be positive for one species and negative for the other. Let us suppose that $(a_{11} - rk_{11}) > (a_{21} - rk_{21})$, i.e. that the net marginal benefit for the first unit of land is higher with species 1 than with species 2. In this case the first square bracket will be positive for f_1 and negative for f_2 . This will ensure a positive value for f_1 . For a positive value of f_2 we would need:

$$|a_{02}[(a_{21} - rk_{21}) - (a_{11} - rk_{11})| < |a_{12}[(a_{21} - rk_{21}) - (a_{01} + a_{02}L)|$$

That is, the difference between the marginal benefit of the first unit of land with species 2 and the marginal benefit with pasture for the last unit (multiplied by the term indicating the variation in the marginal value of species 1) must be larger than the difference between the first unit of land with each one of the two forest species (multiplied by the term indicating the variation in the marginal value for pasture). Of course, in the particular case where $a_{02} = 0$ and marginal pasture value is constant (as assumed in the last part of the general function section) it is easy to show that $f_1^* > 0$ and $f_2^* > 0$, since the first square bracket in the numerator vanishes in both expressions.

To study the relation between f_1 and f_2 in the equilibrium we set (multiplying numerator and denominator by (-1)):

$$\frac{f_1^*}{f_2^*} = \frac{(a_{02} + a_{22})(rk_{11} - a_{11}) - a_{02}rk_{21} + a_{02}a_{21} + a_{22}(a_{01} + a_{02}L)}{(a_{02} + a_{12})(rk_{21} - a_{21}) - a_{02}rk_{11} + a_{02}a_{11} + a_{12}(a_{01} + a_{02}L)}$$

An increase in the constant part of the function describing marginal reforestations costs for species 1 (k_{11}) reduces the ratio f_1^*/f_2^* (it decreases the numerator and increases the denominator). That is, an increase in the plantation costs of species 1, reduces the relative amount of species 1 in the equilibrium.

An increase in the constant part of the function describing marginal reforestations costs for species 1 (k_{21}) increases the ratio f_1^*/f_2^* . That is, an increase in the plantation costs of species 2, reduces the relative amount of species 2 in the equilibrium.

An increase in a_{11} increases the ratio f_1^*/f_2^* . That is, the higher the fix part of the marginal value function of species 1 the higher the relative amount of species 1 in equilibrium.

An increase in a_{21} decreases the ratio f_1^*/f_2^* . The higher the fix part of the marginal value function of species 2 the higher the relative amount of species 2 in equilibrium.

Finally, an increase in the marginal value of the last unit possibly devoted to pasture land $(a_{01} + a_{02}L)$, increases the ratio f_1^*/f_2^* as long as $a_{12} < a_{22}$. That is, as long as the absolute value of the term describing the decrease of species 1 marginal value is higher than this value for species 2.

As expected, the results obtained in the general function section concerning the nature of the equilibrium can be recovered with the quadratic functions. The path of u_i is:

$$\dot{u}_1 = \frac{rk_{11} + rk_{12}u_1 - [a_{11} + a_{12}f_1 - a_{01} - a_{02}(L - f_1 - f_2)]}{k_{12}}$$
(20)

$$\dot{u}_2 = \frac{rk_{21} + rk_{22}u_2 - [a_{21} + a_{22}f_2 - a_{01} - a_{02}(L - f_1 - f_2)]}{k_{22}} \qquad (21)$$

The Jacobian determinant simplifies to:

$$|J_E| = \frac{\partial \dot{u}_1}{\partial f_1} \frac{\partial \dot{u}_2}{\partial f_2} - \frac{\partial \dot{u}_1}{\partial f_2} \frac{\partial \dot{u}_2}{\partial f_1} = \frac{a_{12}a_{22} + a_{12}a_{02} + a_{02}a_{22}}{k_{12}k_{22}} > 0$$

In addition,

$$D = -\frac{\partial \dot{u}_1}{\partial f_1} - \frac{\partial \dot{u}_2}{\partial f_2} = \frac{a_{12} + a_{02}}{k_{12}} + \frac{a_{22} + a_{02}}{k_{22}} < 0$$

And finally we can see that $|J_E| \leq (D/2)^2$ holds since we can re-write this condition as:

$$0 \le \left(\frac{a_{12} + a_{02}}{k_{12}} - \frac{a_{22} + a_{02}}{k_{22}}\right)^2 + 4\frac{a_{02}}{k_{12}}\frac{a_{02}}{k_{22}}$$

Hence, $(f_1, f_2, u_1, u_2) = (f_1^*, f_2^*, 0, 0)$ will be a saddle point for any set of values of parameters in our model.

3.2 Adding carbon sequestration to current incentives

Before analyzing possible measures for the biodiversity-scenic values, which are always highly controversial, we will focus on the current economic incentives for reforestation and on those to be probably implemented in the near future to take into account carbon sequestration. Currently the forest owner focuses on commercial values and on net subsidies (subsidies minus taxes) from the state¹⁰. Subsidies are actually very important in the area under consideration since the Spanish government, within the framework of the EU Common Agricultural Policy reforms, has established a strong incentive for afforestations with corkoaks (these are considered environmentally-friendly subsidies and are not likely to disappear in the near future).

We investigate the impact of carbon prices ranging between 0 and 70 t/C (about $20 \in t/CO_2$). This covers the price range that has been historically observed in the different emerging carbon trading schemes (CCPO, 2006). Nevertheless, future prices might be significantly higher in the future according to simulation models, so that the range analyzed can be seen as conservative.

The first relevant message that comes out from our applied data is that without the current subsidies no reforestation with cork-oaks would take place, even if carbon sequestration is integrated. That is, $(a_{11} - rk_{11}) > (a_{01} + a_{02}L)$ does not hold, and this was a necessary assumption made in the previous section to show that $f_1^* > 0$. Thus, current subsidies are necessary to make cork-oaks a meaningful alternative (these subsidies were set out without taking into account the impact on carbon sequestration).

If we re-write the model previously presented with only one tree species (cork-oak) and pasture, we can study the impact that carbon sequestration incentives would have on cork-oaks if no competition with other species were allowed (this is essentially the same model as the one presented in Van Kooten (2000), although with quadratic functions¹¹). Figure 3 shows the phase diagram

 $^{^{10}}$ We have estimated different functions for these to components of the current incentives to be able to analyze the outcome only with market values; see Table A.3 in the Appendix.

¹¹This phase diagram is not the same as the one shown in Figure 1 since we are rewriting the whole model with only one species, taking thus into account explicitly the space constraint.

without carbon sequestration, and with a carbon value of $70 \in t/C$ (about $20 \in t/C$) t/CO₂) internalized with each of the two methods considered (CFM and TYAM, see Appendix). As can be seen, internalizing carbon sequestration essentially implies to shift outwards the $\dot{u} = 0$ isocline, and this will increase the number of hectares reforested per year and increase the steady-state value of the surface devoted to cork-oak.

[Figure 3]

We now turn to our main model and allow for competition with eucalyptus. As Figure 4 shows, with the current incentives (market values plus net subsidies and a carbon price equal to zero) the equilibrium quantities imply a considerable increase in the surface devoted to euclyptus, although the surface devoted to cork-oak is actually larger than the surface devoted to eucalyptus (28% of the surface would be covered with cork-oaks and 26% with eucalyptus).

Once an incentive for carbon sequestration is introduced using the CFM method the amount of forests increases, especially due to the increase in eucalyptus, although the surface devoted to cork-oaks also increases (as shown in the Appendix we calculate the optimal rotation for eucalyptus taking into account the incentives for carbon sequestration, while we assume that the silviculture for cork-oaks is not changed due to the carbon incentives). Figure 4 shows the equilibrium quantities devoted to cork-oak and eucalyptus for different carbon prices. As shown, with a price of $70 \notin t C$ (about $20 \notin t CO_2$) almost all the surface available is devoted to forest (44% cork-oaks and 47% eucalyptus).

[Figure 4]

If the incentive for carbon sequestration is set up using the TYAM method the forest surface also increases, although less; with the maximum price of 70 \notin /t C considered forests cover 66% of the surface (see Figure 4). Nevertheless, the important difference is that now the increase of forest surface takes place using mainly cork-oaks (with the 70 \in /t C price, cork-oaks cover a 37% of the surface while euclyptus cover 29%). In addition, it has to be taken into account that these results are for the particular equivalence-factor estimated by Moura-Costa and Wilson (2000) of $\varepsilon = 0.0182$. This implies, in our case, that less money goes into the area due to the internalization of carbon sequestration (compared to the CFM). If we would like to see the same amount of money going into the area, the equivalence factor had to be set equal to 0.04^{12} . In this

The steps to draw the phase diagram are essentially the same, so that we will not repeat the whole process (see also Van Kooten (2000)). Let us just add that the f = 0 isocline follows the f_1 axis as before and that the $\dot{u} = 0$ isocline intersects the u_1 axis at $\frac{(a_{11} - rk_{11}) - a_{01} - a_{02}L}{k_{12}}$ and the f_1 axis at $\frac{(a_{11}-rk_{11})-a_{01}-a_{02}L}{-(a_{12}+a_{02})}$.

¹²The precise value of the equivalence factor is highly controversial. In addition, and as stated in the introduction, we are using the TYAM as an example of different accounting methods were the forest owner gets paid for the standing carbon (not for growth).

case, for a carbon price of $70 \in /t C$ up to 46% of the area is reforested with cork-oaks (32% is covered by eucalyptus).

To evaluate the impact on climate change we still need to know what is better, a hectare devoted to cork-oaks or a hectare devoted to eucalyptus. The answer actually depends on the importance given to products outside of the forest (right now the Kyoto framework does not allow to consider carbon stored in harvested wood products, since the decision on this subject matter has been left for future negotiation rounds) If only carbon at the forest is considered, it might well be that on the long run a hectare devoted to cork-oaks is more beneficial, since the amount ultimately stored is higher even if we allow the rotation for eucalyptus to adapt to the carbon incentive (see figure 5). In any case, for eucalyptus most uses would imply a fast decay rate, since the main use is paper pulp.

[Figure 5]

3.3 Adding biodiversity-scenic values

We have estimated biodiversity-scenic values, only for visitors to the Alcornocales Natural Park, using stated preferences techniques. Our approach arguably estimates mainly scenic values, although these values are probably difficult to separate from the biodiversity values perceived by the visitors as associated to the ecosystem favored by species like cork-oaks (this is the reason why we use the term biodiversity-scenic values).

We did a survey with 900 face-to-face interviews to visitors (focus groups and 115 pre-test interviews have also been done). A booklet of 8 pages was given to the interviewees to explain the current situation of the ANP and the impact of a reforestation with cork-oaks or with eucalyptus, for more details on the survey see Caparrós et al. (2006). Table 1 shows that visitors see a reforestation with cork-oaks as 'positive' or 'very-positive' (95%) while they see a reforestation with eucalyptus as 'negative' or 'very-negative' (90%).

[Table 1]

Table 2 shows the models estimated based on a choice and a ranking experiment done to value reforestations with cork-oaks (450 interviews were done with each method). We show the estimations obtained with the choice experiment (CE-cork-oak model) and the estimations obtained pooling the data of the choice experiment and the first rank in the contingent ranking (CP-cork-oak model). The data from the choice and the first rank can be pooled since in Caparrós et al. (2006) it was shown that estimations based on the option chosen and on the first rank are statistically indistinguishable. In the Appendix we show the attributes and the levels used. The data are analyzed using a nested logit model, since the IIA hypothesis was violated (McFadden, 1981). We use the CE-cork-oak model (similar results are obtained using the CP model) to estimate the median willingness to pay for a reforestation using cork-oaks (using Krinsky and Robb's (1986) bootstrapping technique); setting all the attributes but the surface constant (no additional autochthonous species, artificial plantation, no recreational areas, no additional employment). We then estimate the total revenues that could be obtained if the relevant population (visitors) would pay the additional tax. That is, we are assuming that the tax would be set at the limit accepted by 50% of the population but that all the population (visitors) would pay the tax. However, we acknowledge that there is a potential risk for double-counting since one of the reason for the current incentives (subsidies) for cork-oak reforestations are biodiversity-scenic values. Nevertheless, we consider that the current subsidies internalize the WTP of the general public and that the WTP of the visitors is sufficiently higher compared to the one of the general public to make their share on the general subsidies relatively insignificant (although we will check the impact of this assumption in the sensitivity analysis).

[Table 2]

Following the choice or the ranking experiment, half of the interviewees were asked, using an open ended contingent valuation, about a reforestation with cork-oak trees (CV-cork-oak model) and the other 450 subjects were asked about a reforestation with eucalyptus (CV-eucalyptus model). In both cases we made two different questions: one to reforest the equivalent of 20% of current forest surface¹³ and one to reforest 40% of current surface (this was needed to estimate a declining marginal value function). Since the results shown in table 1 (which correspond to the main survey) were already obtained in the pre-test, the interviewees were asked about their willingness to pay (WTP) to ensure a reforestation with cork-oaks and about their WTP to avoid a reforestation with eucalyptus. Table 3 shows the results obtained for these valuation questions (the wording used can be found in the Appendix).

[Table 3]

These are arguably the less reliable values obtained with the different valuation techniques used since: (i) they were made after the choice/ranking experiment, (ii) each respondent faced two different CV questions for two different amounts of land, and (iii) we had to use a relatively 'strange' wording: WTP to avoid a reforestation with eucalyptus. The reason for the first two caveats was that the choice/ranking experiment was actually the main part of the study and we did not want to further complicate the design of our survey instrument (asking only a subsample about each amount of land reforested). The main reason for the wording was that we wanted an estimation of the money that could be made available to compensate forest owners for not using their (hypothetical) right to plant eucalyptus (or any fast growing alien species). In addition, our focus group and our pre-test had shown that a WTA question for reforestations with eucalyptus was not well understood or not taken seriously. Although the CV-eucalyptus model has several caveats the results are probably conservative

 $^{^{13}}$ This was described as needed to counteract current deforestation trends (as in the choice experiment).

since: (i) open ended questions tend to yield lower values, (ii) presenting the question after the choice/ranking experiment probably yielded lower values due to a 'giving fatigue' and (iii) the WTP to avoid question is more conservative than the corresponding WTA question. This is confirmed by the fact that our estimates for cork-oak reforestations values are considerably larger using the choice experiment than using the contingent valuation data.

Figure 6 shows the impact of these biodiversity-scenic values on the results shown in figure 4 (we use the CE-cork-oak and the CV-eucalyptus models, and the median in both cases). As shown, the equilibrium values for cork-oaks are much higher, even without any value for carbon sequestration. As a result, none of the mechanisms for carbon internalization (CFM or TYAM) imply much additional reforestations with cork-oaks, while the CFM would still imply a strong increase in the surface devoted to eucalyptus.

[Figure 6]

To a perform a sensitivity analysis, we first take out the negative value estimated for the reforestations with eucalyptus. The general shape of figure 6 remains unchanged, but with more eucalyptus and slightly less cork-oaks (for a zero carbon price 45% of the surface is reforested with cork-oaks and 20% with eucalyptus). If we take the biodiversity-scenic value for cork-oaks out (and keep the value for eucalyptus) the shape would still be very similar, but starting with 33% of cork-oaks and 15% of eucalyptus for a zero carbon price. In all three cases the most remarkable change with the carbon price is the increase in the share devoted to eucalyptus when carbon is internalized using the CFM.

Figure 7 shows, for a carbon price of $70 \notin /t C$ (aprox. $20 \notin /t CO_2$), the impact of partial or total internalization of the different environmental benefits considered in this article. Whenever biodiversity-scenic values are internalized the amount of surface devoted to cork-oaks is substantially higher than the surface devoted to eucalyptus. If only biodiversity-scenic values are internalized eucalyptus would completely disappear (this is essentially what happens right now due to environmental regulations). On the contrary, if only carbon sequestration is internalized, and this is done with the CFM, the surface of reforested with eucalyptus is larger than the surface reforested with cork-oaks, while the opposite is true if the TYAM method is used. Therefore, the TYAM can be seen as a more conservative way to internalize carbon sequestration which, although implying a lower impact on new forest surface, increases the surface essentially using cork-oaks. This is especially important in areas where biodiversity-scenic values are not properly internalized (actually, most areas).

[Figure 7]

4 Conclusion

This paper has presented and solved qualitatively with general functions an optimal control model to analyze reforestations with two different species, including in the analysis commercial values, carbon sequestration values and biodiversityscenic values. We have discussed the implications of partial or total internalization of environmental values (i.e. carbon sequestration and biodiversity-scenic values), showing that internalizing only carbon sequestration may have negative impacts on biodiversity/scenic values. Nevertheless, the practical relevance of this result can only be determined through applications and we have therefore applied the model to reforestations in the South-west of Spain, comparing reforestations with cork-oaks and reforestations with euclyptus. We have compared the equilibrium outcomes with two different carbon crediting methods: the Carbon Flow Method and the Ton Year Accounting Method; showing that with both methods the forest surface increases, although this increase is more relevant with the CFM method. However, we have also shown that with the CFM method the increase in forest surface takes place essentially using euclyptus while with the TYAM the increase takes place using mainly cork-oaks. Our results have also shown that visitors value reforestations with cork-oaks positively while they consider that reforestations with eucalyptus have a negative impact on their welfare. Furthermore, we have shown that if biodiversity-scenic values (for visitors) were internalized the equilibrium values would imply a significantly larger amount of surface devoted to cork-oaks than the amount devoted to euclyptus (except for high carbon prices internalized using the CFM).

The implications of our results are that if biodiversity-scenic values are properly internalized it may be better to use the CFM, since it tends to increase forest surface more. However, if biodiversity-scenic values are not internalized by markets, as is in fact the case, it may be more appropriate to used a more conservative method like the TYAM, that will increase less forest surface but that will not favor fast growing alien species such as eucalyptus in the South-west of Spain.

5 References

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A Appendix

A.1 Growth and yield models

The empirical illustration focuses on cork oak (*Quercus suber*) and eucalyptus (*Eucalyptus globulus*) plantations over Aljibe Mountains' sand-stone soils (in the Alcornocales Natural Park, South-west of Spain). We use growth functions for three site qualities (high, medium and low). Cork oak growth functions are taken from Sánchez et al. (2005), as well as the initial height and diameter at breast high conditions for different site qualities. Eucalyptus growth functions are our own estimations based on data provided by ENCE¹⁴ for permanent inventory plots in Huelva Mountains (also in the South-west of Spain). For analytical convenience we assume that cork-oak and/or eucalyptus afforestation projects lead to permanent forest. Thus, we analyze an infinite sequence rotations at fixed T_i intervals.

The optimal rotation for eucalyptus is obtained as defined below, taking into account commercial as well as carbon sequestration values (and the particular carbon crediting method under consideration). The functional form of the eucalyptus growth function is:

$$v_i(t) = k t^a e^{-bt} \tag{22}$$

where v_i is the timber volume per hectare measured in m³, subscript *i* indexes the quality of the site (*i* =high, medium, low). The specific site qualities parameters are shown in Table A.1.

[Table A.1]

Carbon sequestration at any moment in time is given by $\alpha v'(t)$, where α is a carbon expansion factor ($\alpha = e_f \phi$), e_f an expansion factor from timber biomass to total biomass (including roots) and ϕ the tons of carbon per m³ of timber biomass. We use a carbon content factor (ϕ) of 0.20 for eucalyptus and an expansion factor of 1.5.

The rotation for cork-oaks is exogenously given. The reason is that cork (bark) is its main woody output (extraction does not imply tree felling) and the striping turn corresponds to the time required for reaching natural cork stoppers thickness (Montero et al., 2005). In the Aljibe area cork is stripped every 9 years, after the first time the cork layer is removed (28 years). The overall rotation,

 $^{^{14}}$ ENCE is a large Iberian and American integral wood-transforming forest company, and we are most grateful for the data provided.

from planting to regeneration fellings (starting after 144 years), is also taken from Montero et al. (2005) since its main purpose is to favor cork production (cork-oak timber has a small value and is not considered while determining rotation). The revenues and costs of the entire rotation cycle of cork oak stands are estimated with the silvicultural treatments and the yields in Montero et al. (2005). Costs and prices are taken from Campos *et al.* (2005).

For cork oak, the specific site carbon sequestration function is estimated for a hectare of cork oak stands, considering Montero et al. (2006) functions that relate cork oak diameter at breast high with different biomass fractions dry weight (trunk, branches, leaves and roots), the carbon content in cork oak biomass (ϕ =0.472; Ibañez et al. (2002)) and the number of standing cork trees along the cork oak rotation cycle. The particular carbon sequestration functions have the same form as eq. (22), but instead of timber volume ($v_i(t)$), the dependent variable is carbon sequestration, measured in carbon tons ($c_i(t)$) per hectare (see Table A.1):

$$c_i(t) = k t^a e^{-bt} (23)$$

Prices for timber, cork and firewood, as well as costs, are assumed to remain constant at 2002 average prices (see Table A.2). Carbon sequestration benefits are analyzed considering a set of carbon prices ranging from 0 to 70 euros per ton of carbon (approximately between 0 and 20 \in /ton of CO₂).

[Table A.2]

A.2 Carbon sequestration accounting methods and optimal rotation

Carbon sequestration revenues are estimated considering two alternative carbon accounting methods: carbon flow and ton year accounting. In both cases we assume that the rotation for eucalyptus is optimized taking into account the carbon incentives while the rotation for cork-oaks stays constant.

A.2.1 Carbon flow method (CFM)

CFM assumes that landowners get paid as carbon is sequestered by biomass growth and pay when carbon is releases through harvesting. The amount of carbon released by harvesting depends on the final use of timber. Van Kooten, et al. (1995) suggest to introduce a parameter (β) that represents the fraction of timber that is harvested but goes into long-term carbon storage structures and landfills (this is the main difference with Englin and Callaway (1993), who assume a decay function).

The present discounted value (PV) of the net benefits from carbon sequestration and timber over all future rotations of eucalyptus at fixed T intervals is (Van Kooten, et al., 1995):

$$PV_{CFM} = \frac{P_F v(T) e^{-rT} - P_c \alpha \left(1 - \beta\right) v(T) e^{-rT} + P_c \alpha \int_0^T v'(t) e^{-rt} dt}{(1 - e^{-rT})}$$
(24)

the first term refers to the value of timber, the second to the price paid for carbon released and the third to the carbon benefits that forest owners get from carbon that is removed from the atmosphere. P_F is the net price of timber cubic meter, P_C represents the value of the credit/tax per carbon ton that is removed from or released into the atmosphere. The FOC is:

$$(P_F + P_c \alpha \beta) v'(T)$$

$$= \frac{r}{(1 - e^{-rT})} \left[(P_F + P_c \alpha \beta) v(T) + r P_c \alpha \int_0^T v(t) e^{-rt} dt \right] - r P_c \alpha v(T).$$
(25)

Cork oak rotation age is given by the normative silvicultural models, but regeneration felling is not the only moment at which carbon is released since cork oaks are subject to different silvicultural treatments that imply biomass extraction (Montero *et al.*, 2005). Given the complexity of the cork oak management we have estimated year to year carbon uptake and release. We have estimated the annual carbon flows assuming that a β fraction of extracted biomass goes into long-term carbon storage structures, and fitted a carbon stock function (Table A.1).

A.2.2 Ton year accounting method (TYAM)

For the TYAM we assume that the government (or a third party via an emission trading system) derives to growers carbon credits adjusted on the basis of the equivalence factor (ε) from sequestering 1 CO₂ ton in the forest biomass for one year. This equivalence factor is estimated based on the cumulative radiative forcing of an emission of CO₂ over a 100-years time horizon. Moura-Costa and Wilson (2000) estimate ε to be 0.0182 t CO₂.

For the TYAM we get the following expression for the present value:

$$PV_{TYAM} = \frac{P_F v(T) e^{-rT} + P_c \alpha \varepsilon \int_0^T v(t) e^{-rt} dt}{(1 - e^{-rT})}$$
(26)

where the second term of eq (26) represents the carbon benefits that forest owners get for having carbon sequestered in their forest (the TYAM does not imply any reimbursement of carbon credits upon harvest). In fact, this method yields a similar result to Hartman's (1973) formula since the standing forest has a value. The FOC used to determine the optimal rotation for the eucalyptus is now:

$$P_F v'(T) + P_c \alpha \varepsilon v(T)$$

$$= \frac{r}{(1 - e^{-rT})} \left[P_F v(T) + P_c \alpha \varepsilon \int_0^T v(t) e^{-rt} dt \right]$$
(27)

For estimating carbon benefits in case of cork oak we use the fitted cork oak carbon sequestration function (Table A.1), and the equivalence factor ε .

A.3 Stated preferences survey

Table A.3 describes the attributes (and the levels) used in the choice/ranking experiment, for more details see Caparrós et al. (2006).

[Table A.3]

The choice/rankings were followed by two contingent valuation question (changing the amount of land reforested). For eucalyptus the wording used was: "iWhat would be the maximum amount that you would be ready to pay more this year as taxes to avoid a reforestation with eucalyptus that would imply to increase the forest area in 20%? (please suppose that only eucalyptus were used, that artificial plantations is used, that no recreational areas are created and that the employment remains constant)."

A.4 Estimation of the quadratic functions

To estimate the quadratic functions for commercial values we have three point estimates (per species), one for each site-quality, since different rates of growth yield different commercial values. Unfortunately, we do not really know the precise surface covered by each of these site-qualities. Since most of the area analyzed is of medium quality for both species, we assume a 25% surface of low quality, a 50% of medium quality and a 25% of high quality. Thus, our results should be seen more as an illustration than as a detailed study (overall trends will be correct, but precise values not so much). For carbon sequestration we also have three point estimates, since the three different growth functions vield different results. For biodiversity-scenic values, we can estimate the value for cork-oaks reforestation using the estimations of the choice experiment (or the pooled data), where the surface reforested enters explicitly in the function estimated (we assume one autochthonous species (cork-oak), artificial reforestation no recreational areas and no additional employment). For eucalyptus (and for cork-oak using the contingent valuation data) we estimate the quadratic function based on the two points estimates given by the subsequent questions (assuming in addition that the function passes through the origin). Table A.4 shows the quadratic functions estimated.

[Table A.4]



Figure 1. Phase-diagram with general functions.



Figure 2. Equilibrium reforestation amounts for species 1 and 2. The functions shown are the marginal value functions for timber (dotted line), timber and carbon sequestration (dashed-dotted line), timber and biodiversity-scenic (dashed line) and timber, carbon and biodiversity-scenic (full line).



Figure 3. Phase-diagram for reforestations with cork-oaks. For the $\dot{u}_1 = 0$ isocline the full line is with commercial values plus subsidies; the dashed line adds carbon sequestration values internalized using the CFM method; and the dotted line adds carbon sequestration values internalized using the TYAM method. Carbon price: 70€t/C.



Figure 4. Figure 6. Equilibrium values of surface reforested with cork-oaks and eucalyptus for different carbon prices (for the CFM and the TYAM). Cork-oak and eucalyptus biodiversity-scenic values for visitors are not internalized.



Figure 5. Carbon in forest biomass for cork-oak (full line), for eucalyptus with a rotation of 10 years (dashed line) and for eucalyptus with a rotation of 14 years (dotted line).



Figure 6. Equilibrium values of surface reforested with cork-oaks and eucalyptus for different carbon prices (for the CFM and the TYAM). Cork-oak and eucalyptus biodiversity-scenic values for visitors are internalized as discussed in the text.



Figure 7. Equilibrium values of surface reforested with cork-oaks and eucalyptus under total or partial internalization of the different environmental values (carbon price: $70 \notin t/C$).

	Could you tell us what is your opinion about a reforestation with in the ANP? (percentage)					
	Cork-oaks	Eucalyptus				
Very negative	0.7	58.9				
Negative	2.5	31.0				
Indifferent	2.2	2.5				
Positive	42.9	6.1				
Very positive	51.8	1.6				

Table 1. Subjective valuation of a reforestation with different species in the Alcornocales Natural Park (ANP)

Attributes	Choice model (CE)	Pooled model (CP)
	Parameter	Parameter
BIO	0.3811	0.3767
	(0.0263)	(0.0209)
TEC	0.3769	0.3250
	(0.0349)	(0.0330)
REC	0.3231	0.3423
	(0.0588)	(0.0932)
EMP	0.0125	0.0135
	(0.0013)	(0.0009)
SUR	0.0666	0.0576
	(0.0069)	(0.0054)
SUR^2	-0.0007	-0.0006
	(0.0001)	(0.0001)
BID	-0.0223	-0.0195
	(0.0024)	(0.0014)
IV $(\alpha_{\text{REF}})^a$	1.5494	1.5161
	(0.8278)	(0.0976)
Ν	3,600	7194
LogL (β)	-2598.12	-5250.86
LogL (0)	-4906.10	-9797.64
ρ^2	0.4698	0.4638

 Table 2.
 Choice and Pooled Nested Logit Models

Standard errors are shown in brackets; N: number of observations.

IV (α_{REF}): inclusive value parameter of the REF branch.

(a) The pooled model combines the choice experiment data and the first rank of the ranking experiment.

(b) Although IV(α_{REF})>1, Herriges and Kling (1996) sufficient condition for local utility maximisation is fulfilled.

***p<.01

	Reforestation current fore (compensate d	to maintain est surface leforestation)	Reforestation to increase a 20% current forest surface			
	WTP to <i>ensure</i>	WTP to <i>avoid</i>	WTP to ensure	WTP to avoid		
	this reforestationthis reforestationwith cork-oakswith eucalyptus		this reforestation	this reforestation		
			with cork-oaks	with eucalyptus		
Total answers	450	450	450	450		
Valid answers	425	408	425	408		
Mean (€)	26.96	24.21	30.49	29.68		
Median (€)	18.00	15.00	20.00	20.00		
Standard deviatio	n 58.43	61.73	60.60	88.65		

Table 3. Willingness to pay to ensure a reforestation with cork-oaks and to avoid a reforestation with eucalyptus in the Alcornocales Natural Park

Table A.1. Parameters of the growth functions for different site qualites

Sites of	Eucalyptus (timber)				Cork-oak (carbon sequestration)					
quality]	Parameters]	R^2				
	k	а	b		k	а	b			
High	2.5062	2.0757	0.0835	0.995	0.9623	1.0467	0.0060	0.651		
	(0.3996)	(0.0857)	(0.0048)		(0.3600)	(0.0967)	(0.0007)			
Medium	1.8528	2.0757	0.0835	0.995	0.8157	1.0241	0.0060	0.667		
	(0.2955)	(0.0857)	(0.0048)		(0.2800)	(0.0891)	(0.0007)			
Low	1.3057	2.0757	0.0835	0.995	1.0223	0.8106	0.0032	0.679		
	(0.2081)	(0.0857)	(0.0048)		(0.3558)	(0.0897)	(0.0006)			

Note: Standard errors are in parenthesis.

* A β of 0.2 is assumed.

Class	Unit	Price	Quantity	Quantity reliant on site qual			
	(U)	(€ U ⁻¹)	(U ha ⁻¹ along the rotation cycle)*				
			High	Medium	Low		
Cork oak							
Summer stripped cork	t	1,100	72.9	54.3	38.8		
Winter cork	t	100	23.6	16.9	10.8		
Firewood	t	30	139.6	106.0	72.6		
Harvesting costs (cork)	t	263.0					
Eucalyptus**							
Timber (farm gate)	m^3	34.8	125.1	92.5	65.1		
Harvesting costs	m^3	10.8					

Table A.2. Outputs, costs and prices (euro, year 2002)

Note: Standard errors are in parenthesis.

* For cork-oak regeneration felling starts after 144 years, in case no carbon is accounted for eucalyptus rotation length is 10 years.
** Timber volume in a €0 price per sequester carbon ton context.

 Table A.3.
 Attributes and levels of the choice/ranking experiments

Attributes	Levels
Biodiversity ^a (BIO)	1; 2; 3; 4
Technique used (TEC)	Natural regeneration; artificial plantation
Number of new recreational areas (REC)	0; 2
Permanent equivalent employees (EMP)	20; 40; 60; 80
Forest surface ensured (SUR)	90% of present surface (10% reduction);
	100% of present surface (same surface);
	120% of present surface (20% increase);
	140% of present surface (40% increase);
Increase in taxes for this year (BID)	6 €; 12 €; 24 €; 48 €

Note: the status quo levels were: no trees, no technique, no additional recreational areas, no employees,

an 80% of the current forest surface ensured (20% reduction) and no additional taxes.

^a Number of autochthonous tree species used, including cork oak.

			Pasture			Quercus			Eucaliptus		
Description	Function	<i>a</i> ₀₁	<i>a</i> ₀₂	R^2	<i>a</i> ₁₁	<i>a</i> ₁₂	R^2	T (years)	<i>a</i> ₂₁	a 22	R^2
Current incentives	W	140.0000	-0.0011		250.1451	-0.0014		10	258.2849	-0.0022	
Commercial (Timber, firewood and/or corl	W/S	140.0000	-0.0011	1.0000	-230.0918	-0.0014	0.9568		266.5725	-0.0022	0.9974
Net subsidies	S				480.2369				-8.2876		
Biodiversity-scenic values											
Choice experiment	В				148.5000	-0.0034	1.0000				
Pooled choice experiment	В				149.5000	-0.0034	1.0000				
Contingent valuation	В				65.0000	-0.0022	1.0000		-50.0000	0.0014	1.0000
Carbon sequestration (CFM)	С										
Price 10 €/tC	С				10.0455	-0.0001	0.9966	11	13.9874	-0.0001	0.9974
Price 20 €/tC	С				20.0909	-0.0002	0.9966	11	27.7986	-0.0002	0.9974
Price 30 €/tC	С				30.1364	-0.0002	0.9966	12	41.6095	-0.0003	0.9974
Price 40 €/tC	С				40.1819	-0.0003	0.9966	13	55.5304	-0.0004	0.9974
Price 50 €/tC	С				50.2273	-0.0004	0.9966	14	69.6338	-0.0006	0.9974
Price 60 €/tC	С				60.2728	-0.0005	0.9966	15	83.9680	-0.0007	0.9974
Price 70 €/tC	С				70.3183	-0.0006	0.9966	15	98.5658	-0.0008	0.9974
Carbon sequestration (TYAM)	С										
Price 10 €/tC	С				3.7911	0.0000	0.9985	10	2.7009	0.0000	0.9974
Price 20 €/tC	С				7.5822	-0.0001	0.9985	10	5.3568	0.0000	0.9974
Price 30 €/tC	С				11.3733	-0.0001	0.9985	11	7.9807	-0.0001	0.9974
Price 40 €/tC	С				15.1645	-0.0001	0.9985	11	10.5843	-0.0001	0.9974
Price 50 €/tC	С				18.9556	-0.0001	0.9985	11	13.1776	-0.0001	0.9974
Price 60 €/tC	С				22.7467	-0.0002	0.9985	12	15.7696	-0.0001	0.9974
Price 70 €/tC	С				26.5378	-0.0002	0.9985	12	18.3683	-0.0001	0.9974
					<i>k</i> ₁₁	k 12			k 21	k 22	
Reforestation costs	K				2419.2848	0.0300			2295.6915	0.0300	

Table A.4. Parameters estimated for the quadratic functions (euros/ha)