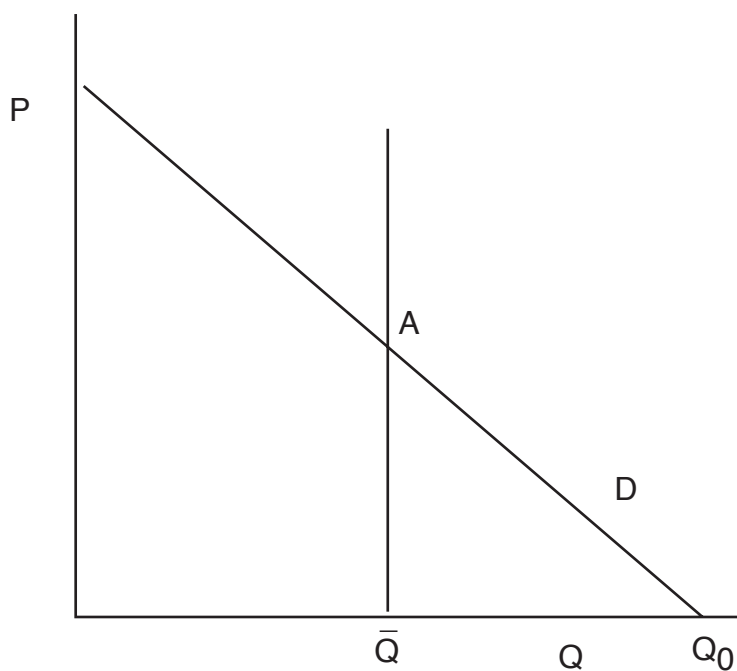


Addendum to Lecture 14

Kyoto Climate Change

The United States needs to reduce CO₂ emissions



D = demand for CO₂

Q_0 = initial level

\bar{Q}_t = target level

$Q_0 - Q_1$ = reduction required

The area $A\bar{Q}Q_0$ = social cost of CO₂ reduction.

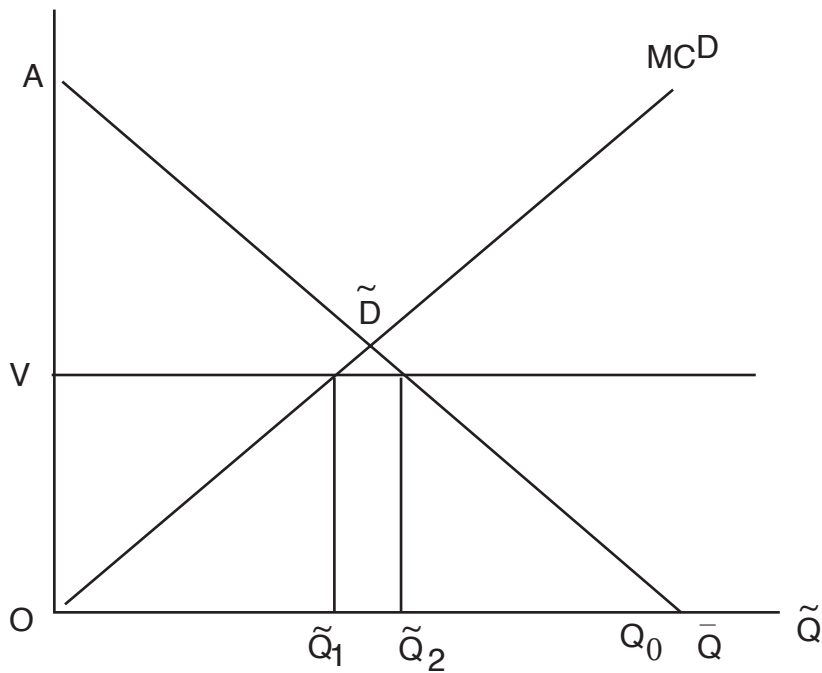
Mechanisms to reduce cost:

1. Purchase CO₂ permits from other countries (Russia), price V .
2. Provide carbon reduction in less-developed countries through the clean developed mechanisms (CDMs),

MC^D = marginal cost of CO₂ provision of CDM.

Using the target levels as benchmarks, let \mathcal{Q} denote consumption of CO₂ beyond \bar{Q} .

\mathcal{D} = demand for \mathcal{Q}



$MC^D(Q^A)$ = marginal cost of quantities available through CDM.

Equilibrium results:

\mathcal{Q}_1 = amount obtained through CDM

$\mathcal{Q}_2 - \mathcal{Q}_1$ = amount purchased on CO₂ market

\mathcal{Q}_2 = extra emissions available beyond \bar{Q} .

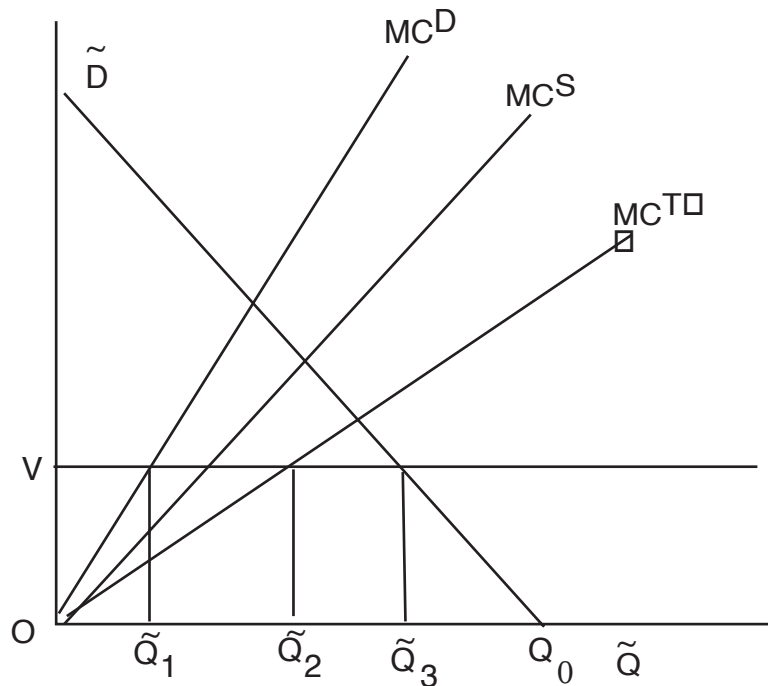
Soil carbon sequestration can be added to the analysis. Let

$$MC^S(\mathcal{Q}) = \text{marginal cost of sequestration}$$

and

$$MC^D(\mathcal{Q}) = \text{marginal cost of CDM.}$$

We can combine the two to form MC^T by horizontal addition. The result is



\mathcal{Q}_1 = quantity provided by CDM

$\mathcal{Q}_2 - \mathcal{Q}_1$ = quantity provided by sequestration

$\mathcal{Q}_3 - \mathcal{Q}_2$ = quantity provided by buying CO_2 permits

\mathcal{Q}_3 = extra CO_2 beyond \bar{Q} .

The Unstable Nature of Soil Carbon

After many years of traditional tillage, an acre of land has exhausted much of its carbon context and can absorb up to (approximately) \bar{S} tons of carbon.

Let S_t be the amount of carbon sequestered in time t , $S_0 = 0$. The amount of carbon sequestered in year t is $X_t = \alpha(\bar{S} - S_t)$.

Assume $\bar{S} = 7$ and $\alpha = .1$.

At year 1, if no tillage is used,

$$X_1 = .7 \text{ tons.}$$

Let ΔY be loss of yield because of low tillage, P be price of output, and V be price of carbon. A farmer will apply no tillage if

$$\underbrace{\alpha V (\bar{S} - S_t)}_{\text{gain from carbon}} - \underbrace{P \Delta Y}_{\text{loss of revenue}} > 0 .$$

(The model is more complex. Low tillage builds soil and increases yield in the long run, but we shall simplify.)

The attractiveness of sequestration declines over time. However, if a farmer switches to traditional tillage, β of S_t is released. If farmers are paid V dollars only for buildup of carbon, a farmer will use no tillage as long as

$$\alpha V (\bar{S} - S_t) > P \Delta Y .$$

There is a critical carbon level in the soil $S^C = \bar{S} - \frac{P \Delta Y}{\alpha V}$, and a farmer will adopt no tillage if $S_t < S^C$.

To maintain carbon in the ground once it is introduced, we need to institute a penalty on tillage activities that will release carbon. Thus, the farmer receives V for sequestered carbon and pays a certain price for released carbon. If the price of the released carbon is also V , a myopic farmer (or a renter) will continue to adopt low tillage when

$$\alpha V(\bar{S} - S_t) + V\beta S_t > P\Delta Y .$$

gain from sequestration
penalty for emission
loss of profit

due to sales

This formula suggests that when a farmer gains and loses based on the emission or sequestration of carbon, the range of adoption increases to include individuals with high carbon storage. The formula suggests that when

$$S_t > \frac{P\Delta Y - \alpha V\bar{S}}{(\beta - \alpha)V} ,$$

the farmer will adopt low tillage.

If $P\Delta Y$ is very small, the denominator is negative, and the farmer will always adopt. Higher carbon pay and lower output price will enhance adoption.