

**Micro-finance institutions**

**1. MFIs and their borrowers**

**1.1. The principles of group lending**

- Grameen Bank
  - Other MFIs
  - The basic rules of micro-finance for the poor:
    - small loans at start and steep increase in loan size
    - no physical collateral
    - intensive screening and monitoring by agents
  - The basic rules of group lending: same plus:
    - self-selection in groups (SS)
    - joint liability (JL)
  - The usual arguments for group lending:
    - SS + JL  $\Rightarrow$  eliminate bad borrowers (AS)
    - SS among people that know each other  $\Rightarrow$  Social sanctions for enforcement  $\Rightarrow$  limit MH in willingness to pay and in choice of projects.
- Both allow to maintain access to the poor and high repayment rates

**1.2. The lending problem**

- Moral hazard in repayment:  
 Could be curtailed by either collateral or dynamic incentives. Hence not such an issue. The real problem is the need for insurance.

Investment of 1 unit  $\Rightarrow X$  with probability  $p$  and 0 with probability  $(1 - p)$ .  
 Assume no other resources to repay (hence necessary limited liability).  
 Repayment  $r$  (includes principal).

				Net return		
				Returns:	Collateral	Future
$(1-p)$	Fails	Default		0	$-C$	0
$p$	Success	Repay		$X - r$	$X - r$	$X - r + F$
		Unwilling		$X$	$X - C$	$X$

MH eliminated if  $C > r$  (but then limited liability is de facto cancelled) or  $F > r$ .  
 But this does not address the fundamental risk of a bad return, and the consequent loss of access to credit.

- Limited liability and adverse selection:  
Would need differentiated contracts. With asymmetric information, cross subsidization of risky borrowers by safe borrowers. Problem to keep safe borrowers.

- 2 types of individual

$$\begin{array}{cccc} R & X_R & p_R & \mu \\ S & X_S & p_S & (1-\mu) \end{array} \quad (\mu \text{ proportion in population})$$

$$p_S > p_R, X_S < X_R.$$

Bank: 0 profit, cost of money :  $\rho$  (including principal)

- First best under perfect information is interest rate discrimination:  $r_i = \rho/p_i$ ,
- Under asymmetric information: pooling  $\Rightarrow$  interest rate at an intermediate level.

$$\mu p_R r + (1-\mu) p_S r = \rho$$

$$\Rightarrow r = \frac{\rho}{\mu p_R + (1-\mu) p_S} \quad \text{Hence } r_S < r < r_R$$

Cross-subsidization of risky loans by safe loans.

Participation of borrower  $i$  for  $p_i X_i \geq p_i r$

If projects are just profitable,  $p_S X_S = p_R X_R = \rho$ , then  $S$  borrowers are driven out. (Lemons)

- Exercise: For reference, find an efficient separating contract.

### 1.3. Joint liability with a unique contract: produces interest rate discrimination, which improves efficiency and the pool of borrowers (Ghatak, EJ 2000)

- JL and SS induce assortative matching (homogenous groups)  
JL: payment of own share  $r$  if successful, and part of other's share  $c$  if other fails.  
Utility for  $i$  associated with  $j$ :

$$U_{ij} = p_i X_i - p_i \left( r + (1-p_j) c \right)$$

$$\text{Loss to } S \text{ for accepting } R: T_S = p_S (p_S - p_R) c$$

$$\text{Gain to } R \text{ for teaming with } S: B_R = p_R (p_S - p_R) c < T_S$$

Hence heterogenous groups are not possible, since  $R$  cannot compensate  $S$ .

Notice: This model has no cost to losing access to credit. Show that heterogenous groups are possible if there is future benefit in access to credit (Sadoulet, 2000)

- Hence interest rate discrimination:

Payment by  $i$ :  $P_i = p_i(r + (1 - p_i)c)$

Difference:  $P_R - P_S = (p_S - p_R)((p_S + p_R - 1)c - r)$  increases with  $c$ .

As  $c$  increases, efficiency in allocation of resources improves.

$P_R$  however remains lower than  $P_S$  for  $c < \frac{r}{p_S + p_R - 1}$ . Hence usually cannot reach full efficiency.

- Equilibrium contract:

Zero profit for bank:  $\mu p_R(r + (1 - p_R)c) + (1 - \mu)p_S(r + (1 - p_S)c) = \rho$

$$\Rightarrow r = \frac{\rho}{\bar{p}} + c \left( \frac{\mu p_R^2 + (1 - \mu)p_S^2}{\bar{p}} - 1 \right), \text{ where } \bar{p} = \mu p_R + (1 - \mu)p_S$$

- Pool of borrowers:

Payment by  $i$ :  $P_i = \rho \frac{P_i}{\bar{p}} - c \frac{P_S P_R}{\bar{p}} (p_i - \bar{p})$

Participation constraint:  $P_i \leq p_i X_i$

Hence  $c$  lowers the participation constraint for  $S$  and raises it for  $R$

$\Rightarrow$  improves efficiency in allocation of funds.

#### 1.4. Joint liability as a screening device, with a menu of contracts (Ghatak, EJ 2000)

- The contract:

Bank offers a menu  $\{(r_S, c_S), (r_R, c_R)\}$

$U_{ij}(k) = p_i X_i - p_i (r_k + (1 - p_j)c_k)$ , utility to  $i$ , associated with  $j$ , in contract  $(r_k, c_k)$

Constraints:

- zero-profit on each type of loan:  $p_i(r_i + (1 - p_i)c_i) = \rho$

- participation constraint:  $U_{ii}(i) = p_i X_i - p_i(r_i + (1 - p_i)c_i) \geq 0$

- incentive compatibility:  $U_{ii}(i) \geq U_{ii}(j)$

- limited liability constraint:  $r_i + c_i \leq X_i$

- Incentive compatibility constraint  $\Rightarrow$  assortative matching:

$$U_{SS}(S) - U_{SR}(S) > U_{RS}(S) - U_{RR}(R)$$

- Optimal contract:

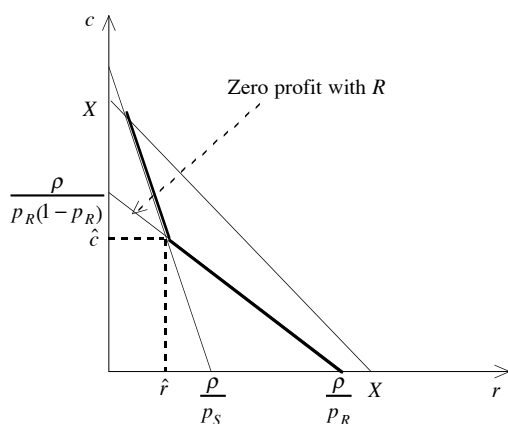
Let  $(\hat{r}, \hat{c})$  be the efficient pooling contract solution of 1.3 above:

$$\hat{c} = \frac{\hat{r}}{p_S + p_R - 1} \text{ and } \hat{r} \frac{p_S p_R}{p_S + p_R - 1} = \rho, \text{ (which satisfy: } p_i (\hat{r} + (1 - p_i) \hat{c}) = \rho \text{)}$$

Then there exists a separating contract  $\{(r_S, c_S), (r_R, c_R)\}$ , in which:

$$r_S < \hat{r} < r_R \text{ and } c_R < \hat{c} < c_S$$

Notice, however, that in this contract,  $\hat{c} > \hat{r}$ , and henceforth  $c_S > r_S$



### 1.5. Joint liability induces the choice of safer projects (Ghatak & Guinnane, JDE 99)

One type of borrower :  $X$  with probability  $p$ , and 0 with probability  $(1-p)$

Borrower/agent can choose  $p$ , at cost  $\frac{1}{2} \gamma p^2$

Bank/principal sets the interest rate for 0 profit.

- Individual loan without limited liability (first best):

$$p = \arg \max \left( pX - r - \frac{1}{2} \gamma p^2 \right) = \frac{X}{\gamma} \text{ and bank sets } r = \rho$$

- Individual loan with limited liability:

$$p = \arg \max \left( p(X - r) - \frac{1}{2} \gamma p^2 \right) = \frac{X - r}{\gamma} < \frac{X}{\gamma}$$

Bank's zero profit:  $pr = \rho \Rightarrow p^*$  solution of  $\gamma p^2 - pX + \rho = 0$ .

- Non-cooperative group playing Nash:

Reaction function:

$$p_i = \arg \max \left( p_i (X - r) - p_i (1 - p_j) c - \frac{1}{2} \gamma p_i^2 \right) = \frac{X - r - c}{\gamma} + p_j \frac{c}{\gamma}$$

Nash non-coop solution:  $p_i = \frac{X - r - c}{\gamma - c}$

Bank's zero profit:  $pr + p(1 - p)c = \rho$

$\Rightarrow p^*$  solution of  $\gamma p^2 - pX + \rho = 0$ , same as individual.

- Cooperative group:

Joint maximization:

$$p_i = \arg \max \left( p(X - r) - p(1 - p)c - \frac{1}{2} \gamma p^2 \right) = \frac{X - r - c}{\gamma - 2c}$$

Bank's zero profit:  $pr + p(1 - p)c = \rho$

$\Rightarrow p^{**}$  solution of  $(\gamma - c)p^2 - pX + \rho = 0$ .

$p^{**} > p^*$  and repayment rate of each individual is higher than under individual loans.

**Conclusion:** Group credit creates a mechanism for mutual insurance  $\Rightarrow$  improves efficiency in resource allocation towards safer borrowers and safer projects.  
However: transfers insurance from (risk-neutral) Bank to (risk-averse) borrowers

**References:**

Ghatak, M. "Screening by the Company you Keep: Joint Liability Lending and the Peer Monitoring Effect." *Economic Journal*, 2000 July, V110 N465:601-31.

Ghatak, M; Guinnane, TW. "The economics of lending with joint liability: theory and practice." *Journal of Development Economics* 1999 OCT, V60 N1:195-228.